

Abstract Interpretation and Properties of C Programs

EJCP 2018

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Context

Overview of Static Analysis

Analyzing C code with Frama-C

EVA Plugin

- ▶ Software is more and more pervasive in embedded systems...
- ▶ ...and keeps getting larger
- ▶ Tests and code review too costly beyond a certain size and coverage criterion
- ▶ Need for **correct** tools
 - ✓ Detect all potential issues
 - ✗ May issue spurious warnings
 - ✗ Impossible for an automated tool to warn for all real issues and only for them (Rice theorem)

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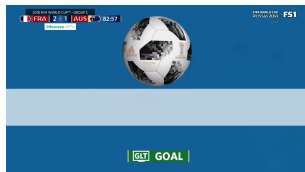
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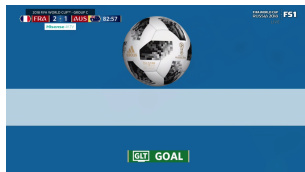
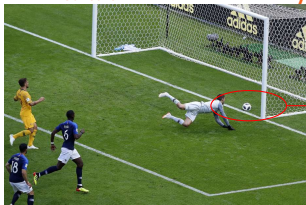
Abstract Interpretation in two pictures



Abstract interpretation is about

- ▶ abstracting away information
- ▶ ensuring answer in a reasonable time
- ▶ while retaining adequate precision
- ▶ and guaranteeing correct answers

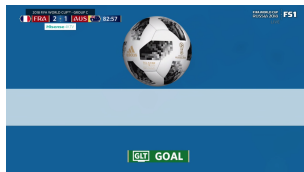
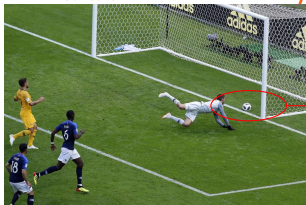
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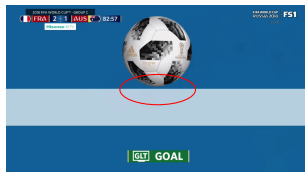
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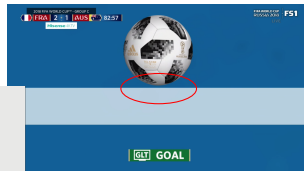
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Abstract Interpretation in two pictures



Foot : après de nouveaux bugs, la Ligue suspend la "goal-line technology" jusqu'à nouvel ordre

Les derniers dysfonctionnements ont été constatés, mercredi soir, lors des quarts de finale de Coupe de la Ligue, entre Amiens-PSG et Angers-Montpellier.



Abstract interpretation is about

- ▶ abstracting away information
- ▶ ensuring answer in a reasonable time
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Surréaliste : un bug de la goal-line force l'arbitre à accorder puis annuler un but à Troyes

Context

Overview of Static Analysis

Static Analysis Framework

Abstract Interpretation

Analyzing C code with Frama-C

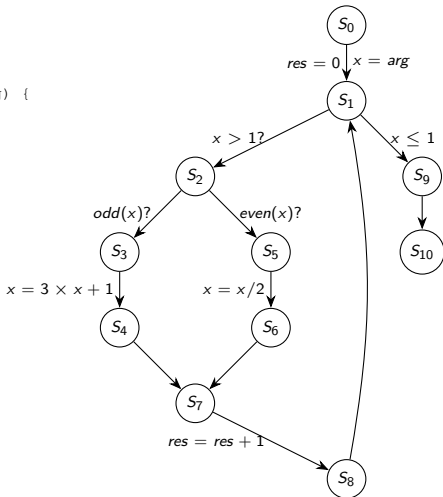
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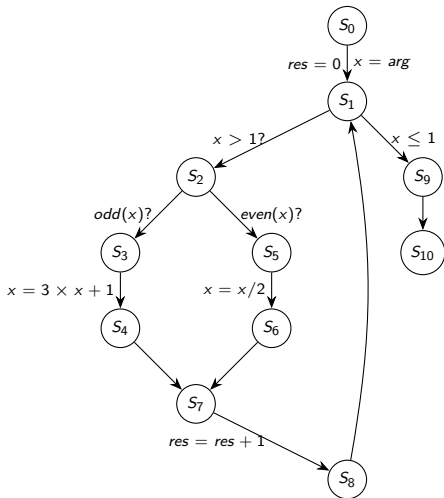
Control-Flow Graph

```

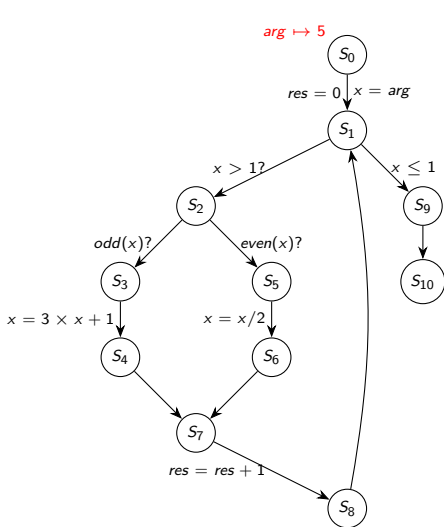
mpz_ptr syracuse(mpz_t res, const mpz_t arg) {
  mpz_t x;
  mpz_init_set_ui(res, 0UL);
  mpz_init_set(x, arg);
  while (mpz_cmp_ui(x, 1UL) > 0) {
    mpz_out_str(stdout, 10, x);
    putchar('\n');
    if (mpz_odd_p(x)) {
      mpz_mul_ui(x, x, 3UL);
      mpz_add_ui(x, x, 1UL);
    } else {
      mpz_cdiv_q_ui(x, x, 2UL);
    }
    mpz_add_ui(res, res, 1UL);
  }
  mpz_clear(x);
  return res;
}

```



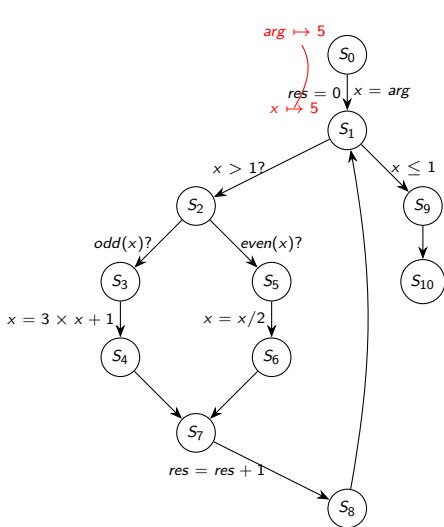


- ▶ Initial state on start node
- ▶ Transfer functions across edges
- ✗ infinite number of traces
- ✗ some traces might be infinite



S_0
 $arg \mapsto 5$

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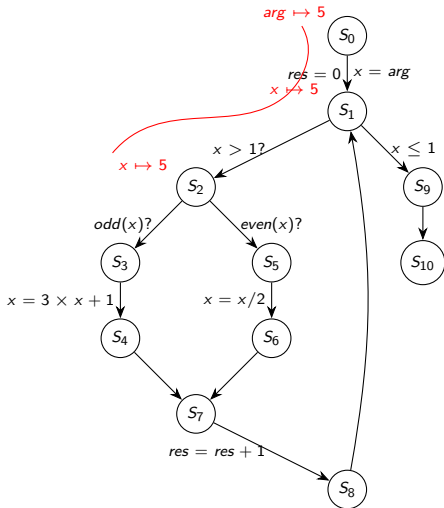


$$\begin{array}{ccc}
 s_0 & & s_1 \\
 arg \mapsto 5 & \Longrightarrow & x \mapsto 5 \\
 & & res \mapsto 0
 \end{array}$$

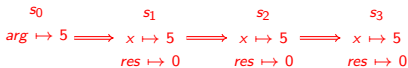
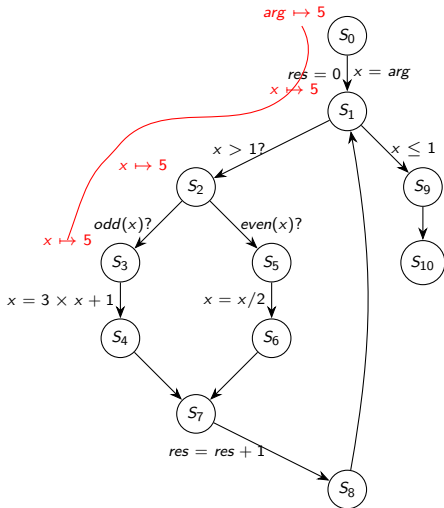
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Trace Semantics

$$\begin{array}{c}
 s_0 \qquad \qquad s_1 \qquad \qquad s_2 \\
 arg \mapsto 5 \implies x \mapsto 5 \implies x \mapsto 5 \\
 \qquad \qquad \qquad res \mapsto 0 \qquad \qquad res \mapsto 0
 \end{array}$$

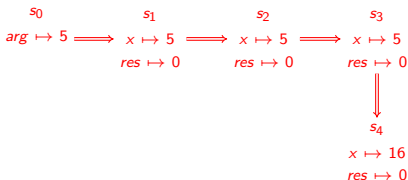
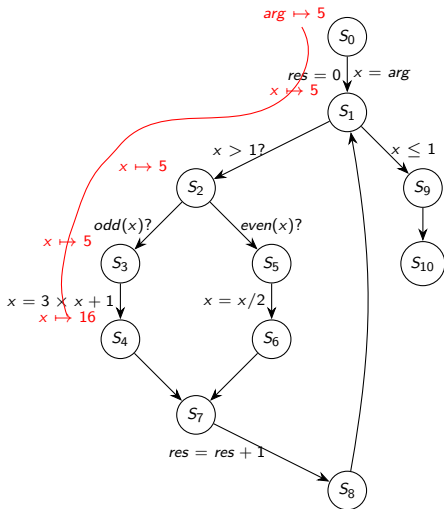


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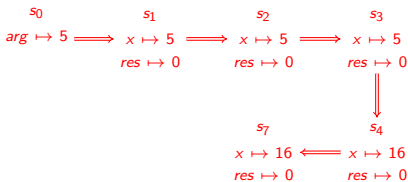
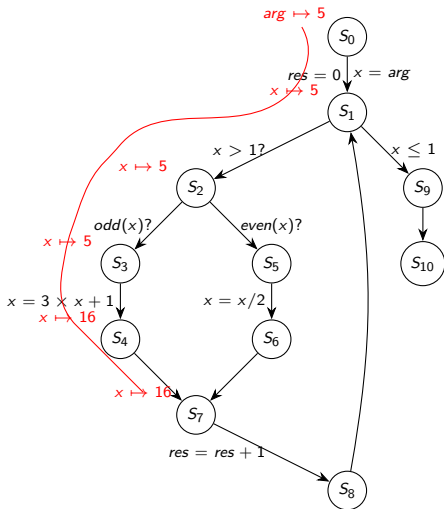
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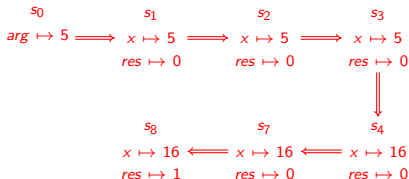
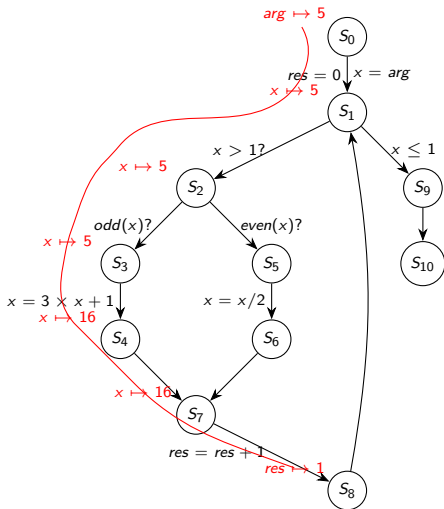
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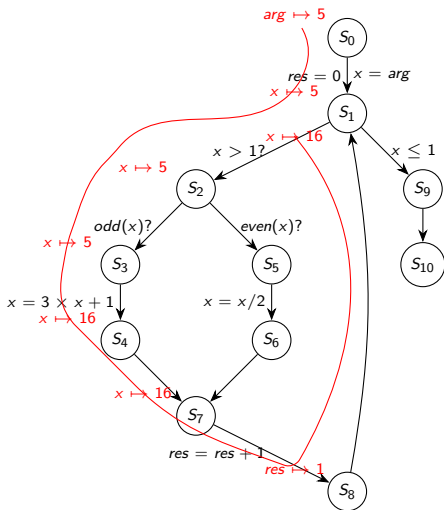


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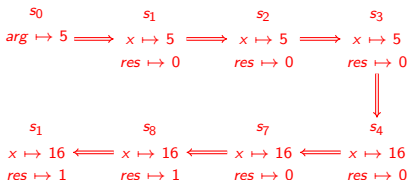
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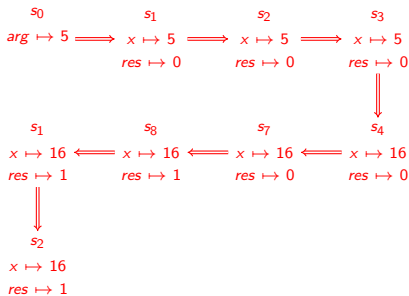
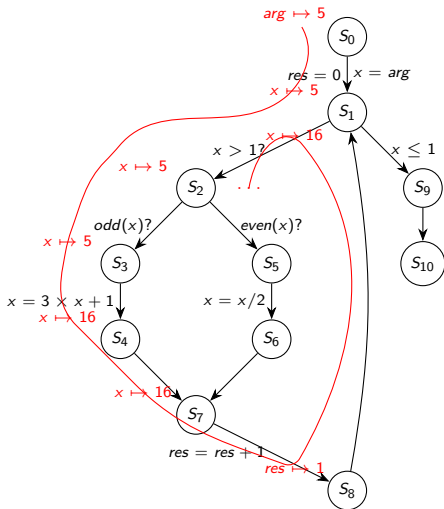


Trace Semantics



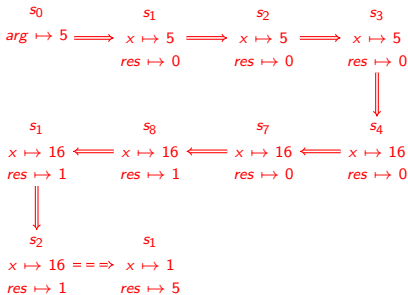
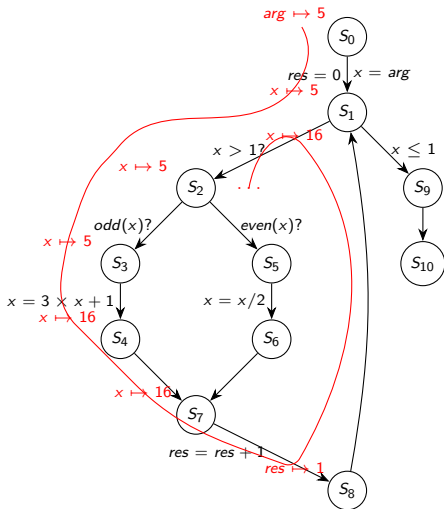
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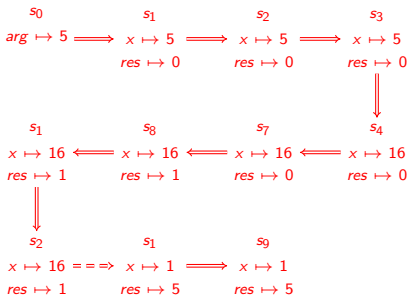
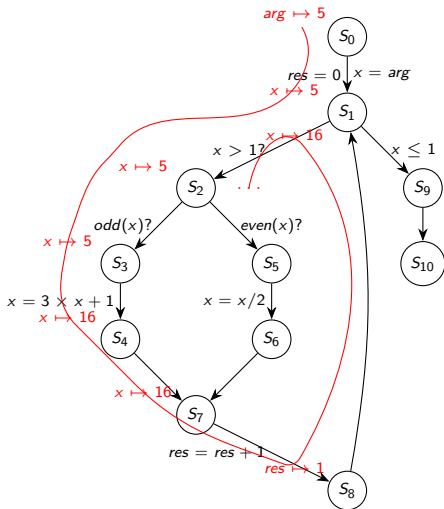
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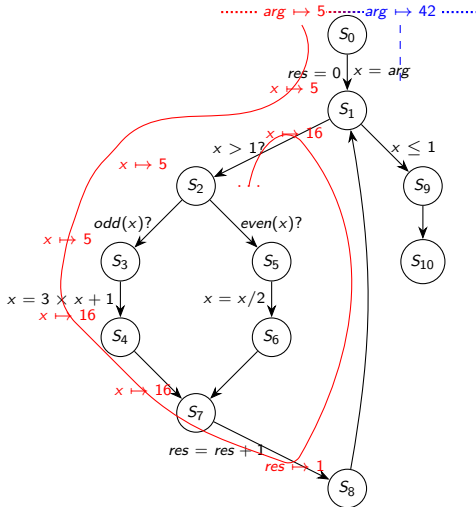


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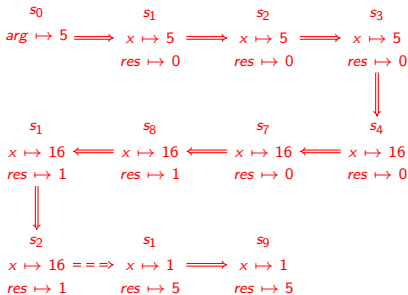
Trace Semantics



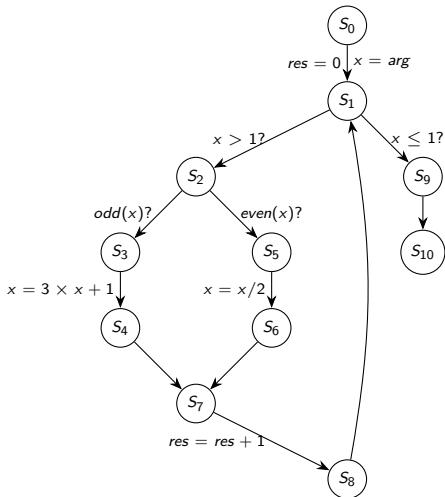
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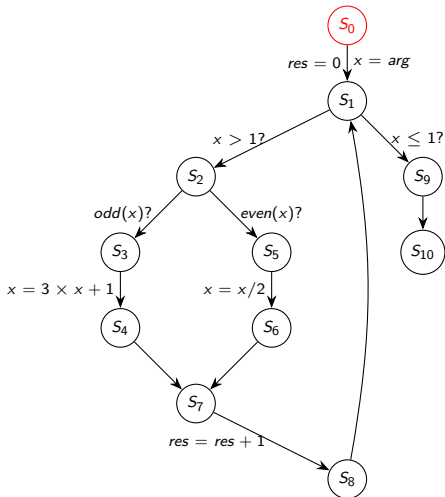


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- ▶ From the set of all traces to set of all states
- ▶ multiple predecessors: take union
- ▶ lose “temporal” relations
- ▶ fixpoint computation
- ▶ may not terminate

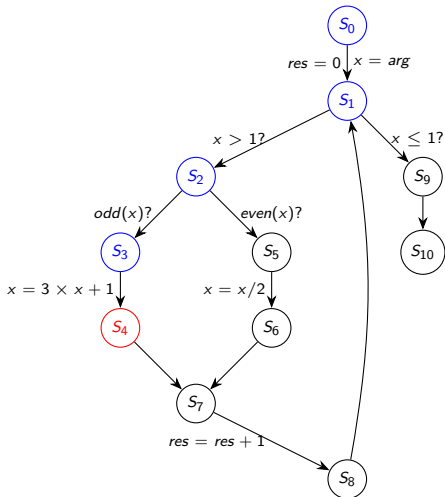
Collecting Semantics



$S_0 \mapsto arg \in \mathbb{Z}$

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Collecting Semantics



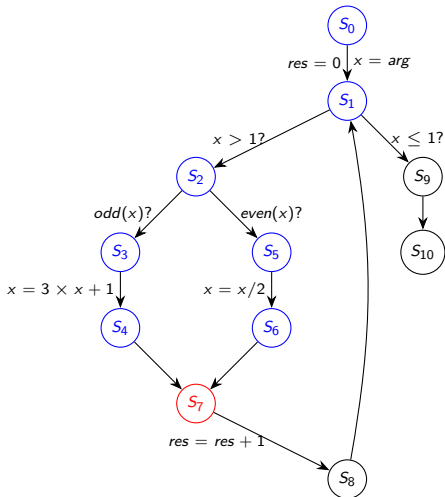
$$S_3 \mapsto \{(x, res) \mid x = 2k + 1, res = 0\}$$



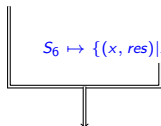
$$S_4 \mapsto \{(x, res) \mid x = 6k + 2, res = 0\}$$

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Collecting Semantics



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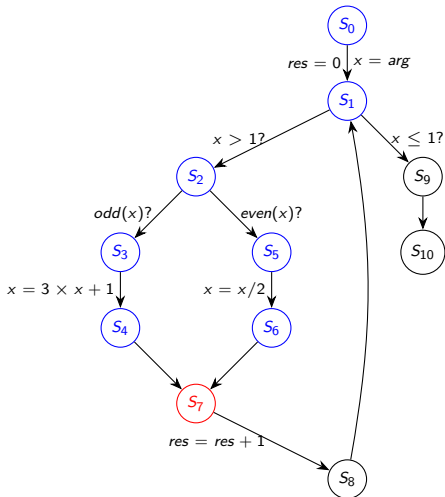


$$S_6 \mapsto \{(x, res) \mid x = k, res = 0\}$$

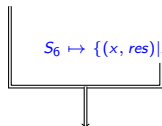
$$S_7 \mapsto \{(x, res) \mid x = k, res = 0\}$$

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Collecting Semantics



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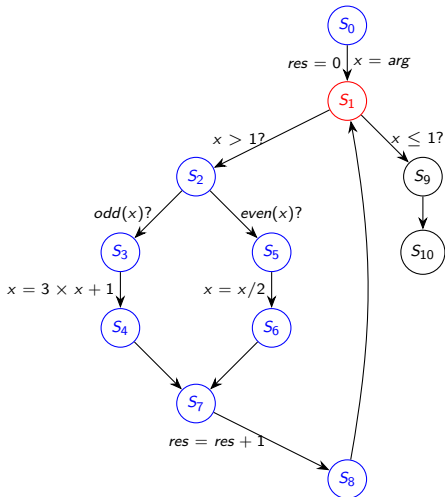


$$S_6 \mapsto \{(x, res) \mid x = k, res = 0\}$$

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Collecting Semantics



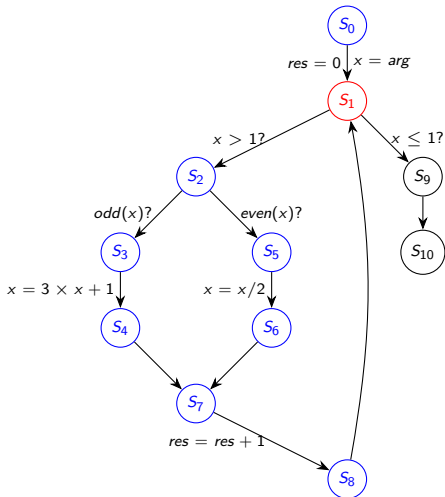
$$S_1 \mapsto \{(x, res) \mid x = k, res = 0\}$$

$$S_8 \mapsto \{(x, res) \mid x = k, res = 1\}$$

$$S_1 \mapsto \{(x, res) \mid x = k, res \in \{0, 1\}\}$$

- ▶ From the set of all traces to set of all states
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- ▶ **fixpoint computation**
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Collecting Semantics



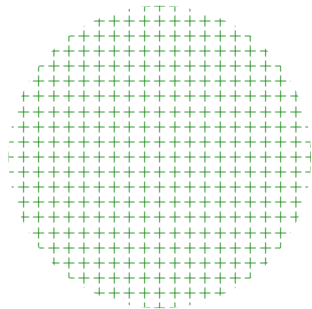
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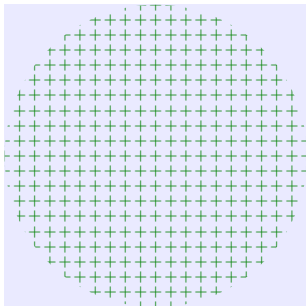
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Static Analysis framework



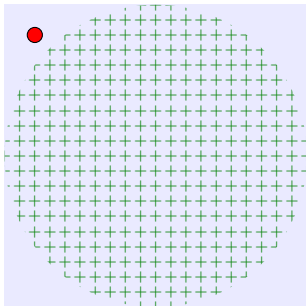
- ▶ Replace set of states ...
- ▶ ... by one element in an abstract lattice
- ▶ Over-approximation and false alarms
- ▶ Trade-off between precision and computation time

Static Analysis framework



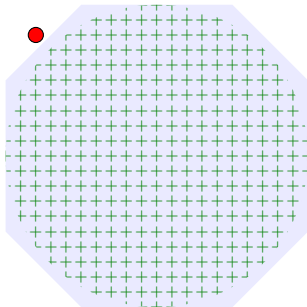
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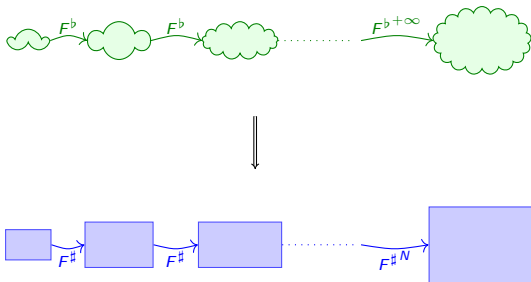
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Correctness and Termination



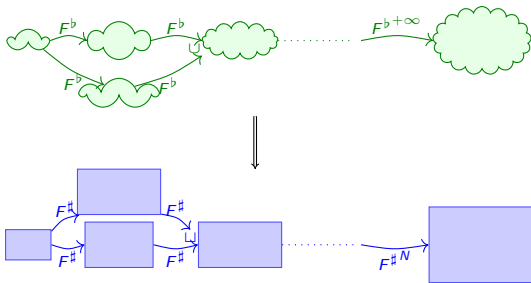
- ▶ Abstract transfer functions $F^\#$
- ▶ Merge abstract states for nodes with multiple predecessors
- ▶ **Correction:** Do we include all concrete states in the end?
- ▶ **Termination:** Converge in a finite number of steps
- ▶ **Abstract interpretation:** A systematic way to build correct and terminating analyses

Correctness and Termination



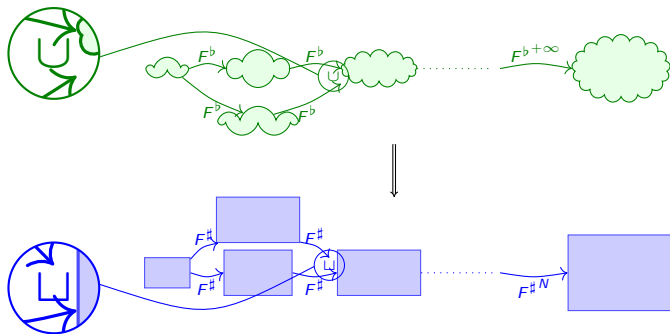
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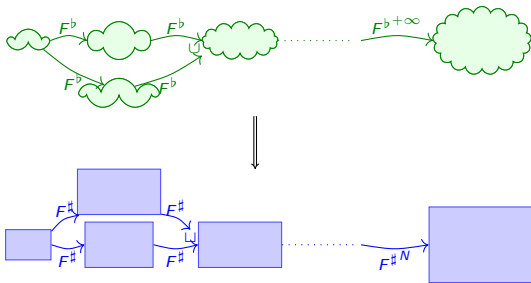
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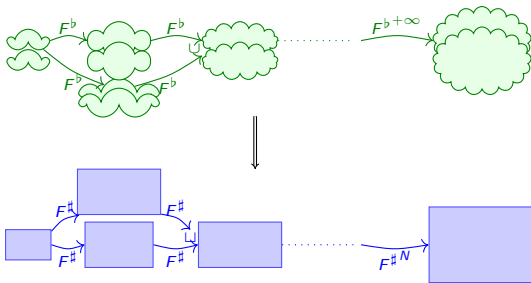
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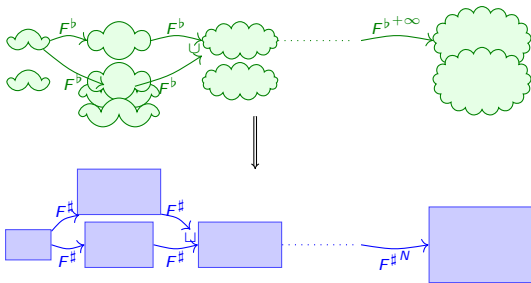
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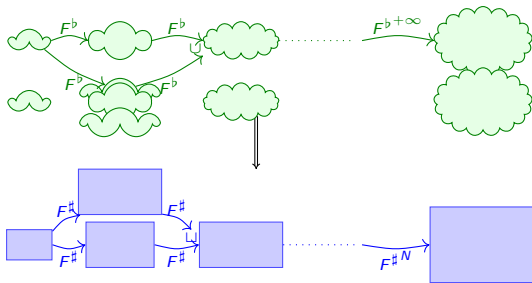
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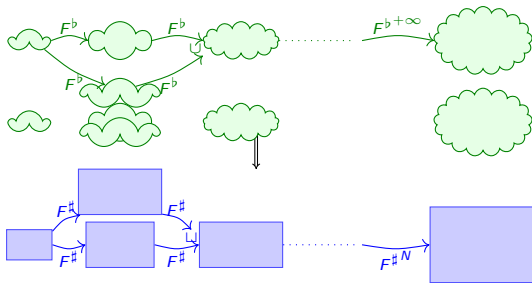
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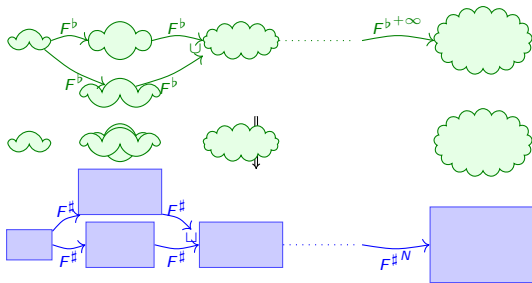
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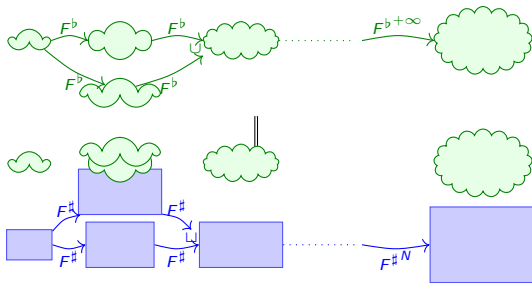
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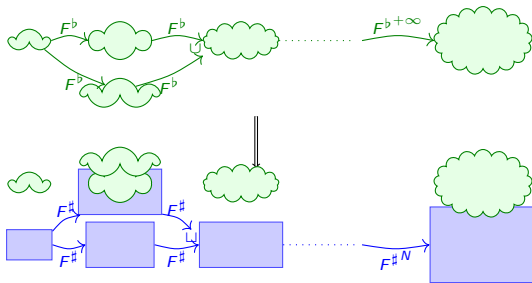
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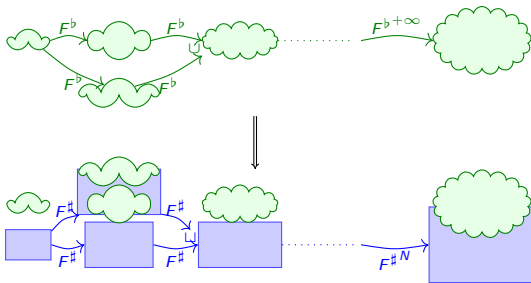
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- ▶ **Correction:** Do we include all concrete states in the end?
- ▶ **Termination:** Converge in a finite number of steps
- ▶ **Abstract interpretation:** A systematic way to build correct and terminating analyses

Correctness and Termination



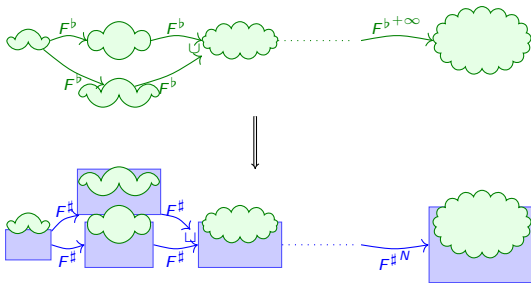
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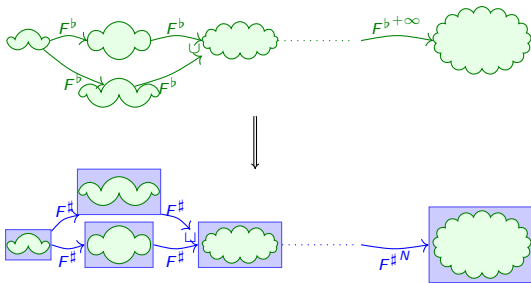
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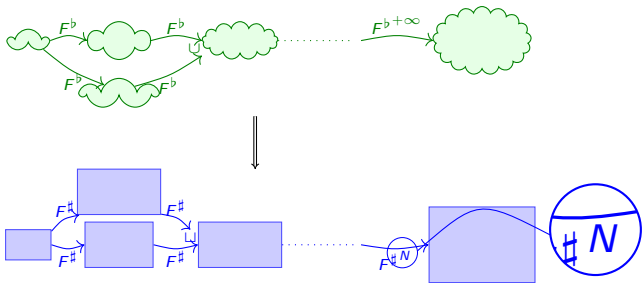
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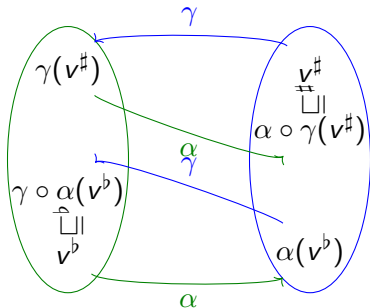
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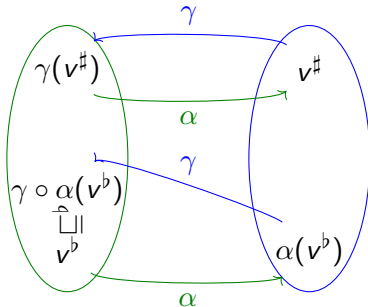
Galois connection and insertion

- ▶ α returns an abstraction from a set of concrete states
- ▶ γ returns the set of concrete states corresponding to an abstraction
- ▶ Following properties must hold:
 1. α and γ are **monotonic**
 2. $\forall v^b \in L^b, v^b \sqsubseteq^b (\gamma \circ \alpha)(v^b)$
 3. $\forall v^\# \in L^\#, (\alpha \circ \gamma)(v^\#) \sqsubseteq v^\#$
- ▶ **Theorem [Cousot]:** If $F^\# \sqsupseteq \alpha \circ F^b \circ \gamma$, abstraction is **correct**.



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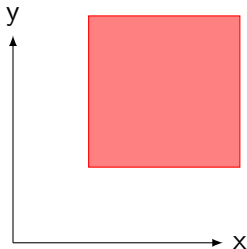


Relational and Non-relational Lattices

Non-relational domain

- ▶ Considers each variable independently
- ✓ Simpler and less costly
- ✗ lose properties over 2+ variables

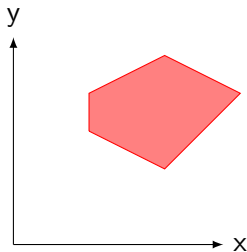
Example: intervals

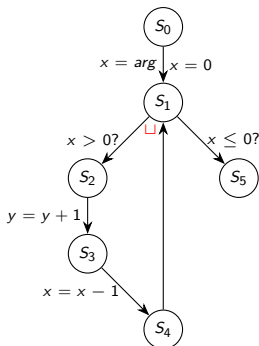


Relational domain

- ▶ Considers several variables at once
- ✓ More precise
- ✗ More complex and costly

Example: Polyhedra

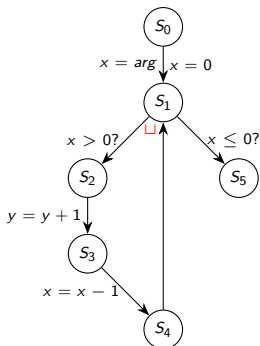




$$S_1 \text{ (before)} \quad S_4 \quad = \quad S_1 \text{ (after)} \\
 y \in [0; 0] \sqcup [1; 1] = [0; 1]$$

- ▶ for loop nodes, state grows slowly at each step
- ▶ convergence could require infinite time
- ▶ replace \sqcup with widening operator ∇ :

correctness $x \sqcup y \sqsubseteq x \nabla y$
 termination no infinitely growing sequence
 $x_0 \nabla x_1 \nabla \dots \nabla x_n \dots$

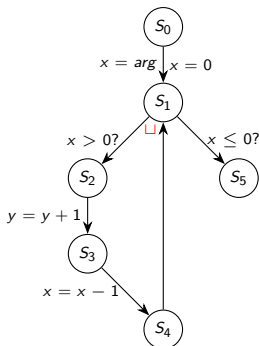


$$S_1 \text{ (before)} \quad S_4 \quad = \quad S_1 \text{ (after)}$$

$$y \in [0; 1] \sqcup [1; 2] = [0; 2]$$

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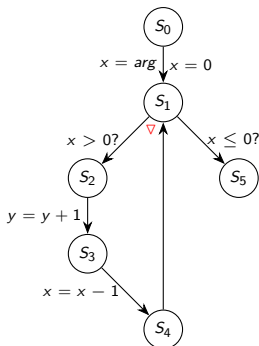


$$S_1 \text{ (before)} \quad S_4 \quad = \quad S_1 \text{ (after)}$$

$$y \in [0; 2] \sqcup [1; 3] = [0; 3]$$

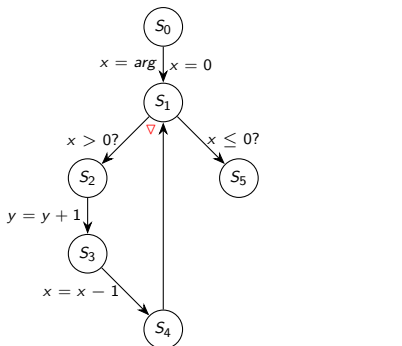
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S_1 (before) S_4 S_1 (after)
 $y \in [0; 2]$ ∇ $[1; 3]$ $= [0; +\infty]$

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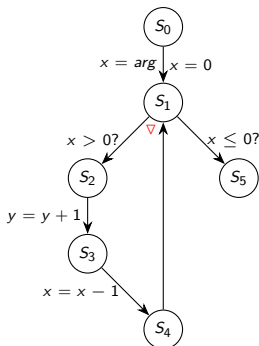
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$$S_1 \text{ (before)} \quad S_4 \quad S_1 \text{ (after)}$$

$$y \in [0; 2] \quad \nabla \quad [1; 3] = [0; +\infty]$$

lower bound stable:
don't change



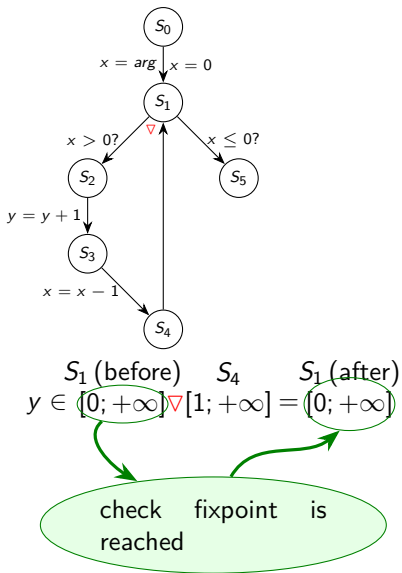
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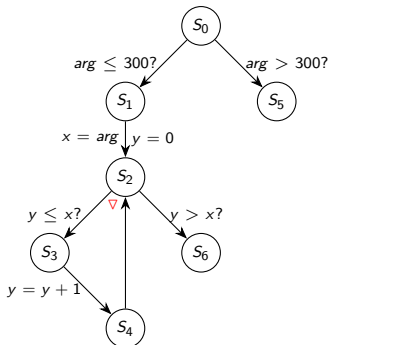
correctness $x \sqcup y \sqsubseteq x \nabla y$
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upper bound grows:
widen interval



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Recover some precision

- ▶ Widening can be very coarse
- ▶ Use **narrowing** after reaching fixpoint:

correctness $y \sqsubseteq (x \Delta y) \sqsubseteq x$

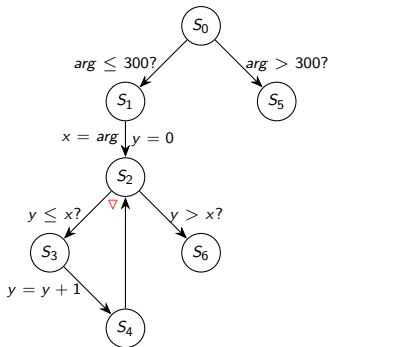
termination no infinitely decreasing sequence

- ▶ In practice, very often better to directly improve widening

$$S_2 \text{ (before)} \quad S_4 \quad S_2 \text{ (after)}$$

$$y \in [0; 0] \quad \nabla \quad [1; 1] \quad = \quad [0; +\infty]$$

widen and propagate
new bound



S_2 (before) S_4 S_2 (after)
 $y \in [0; +\infty] \triangleright [1, 301] = [0; +\infty]$

∞ may be too much
try to narrow it down

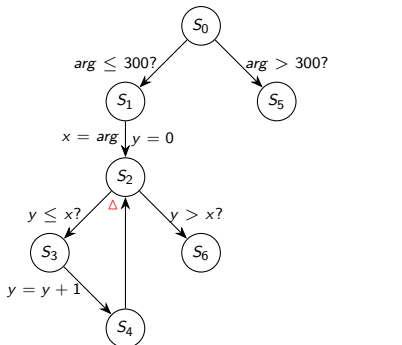
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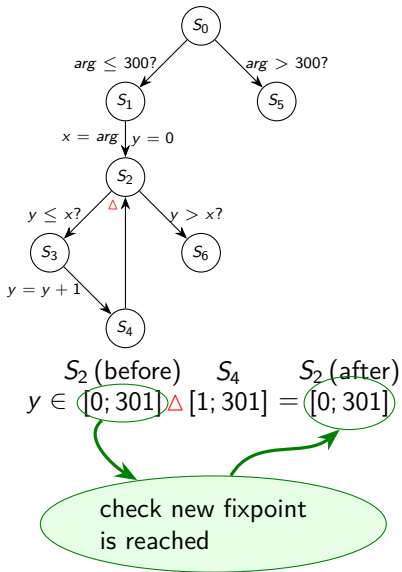
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$$S_2 \text{ (before)} \quad S_4 \quad S_2 \text{ (after)}$$

$$y \in [0; +\infty] \Delta [1; 301] = [0; 301]$$

Candidate bound
to be propagated



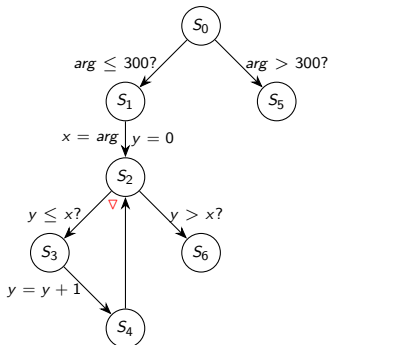
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widen and propagate
new bound

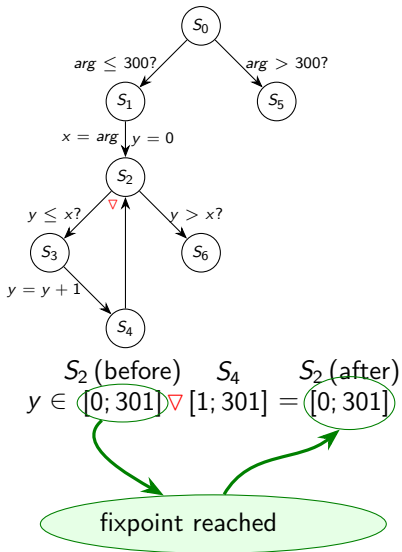
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Question

We have information from two domains:

Intervals:

▶ $x \in [0; 20]$

▶ $y \in [5; 10]$

Octagons:

$$0 \leq x - y \leq 20$$

What can be said about x and y ?

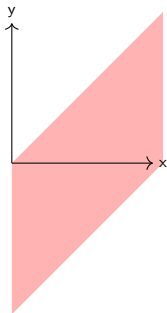
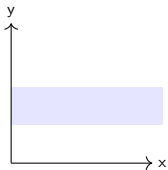
Answers

▶ a $x \in [0; 20], y \in [5; 10]; 0 \leq x - y \leq 20$

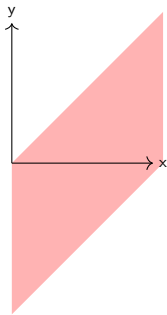
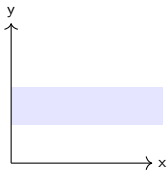
▶ b $x \in [5; 20], y \in [5; 10], 0 \leq x - y \leq 15$

▶ c $x \in [5; 20], y \in [5; 10], 0 \leq x - y \leq 10$

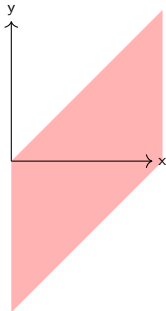
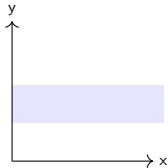
▶ d $x \in [5; 20], y \in [0; 20], 0 \leq x - y \leq 20$



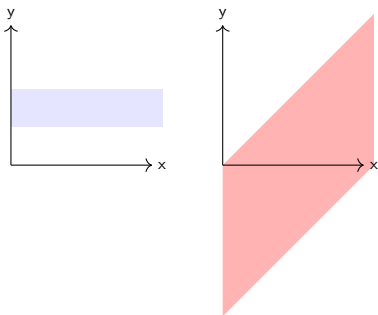
- ▶ Combining abstract domains
- ▶ **reduce** abstract value from one domain using information from the other
- ✗ In practice, not as simple and generic as it looks
- ✗ Combining transfer function is complex



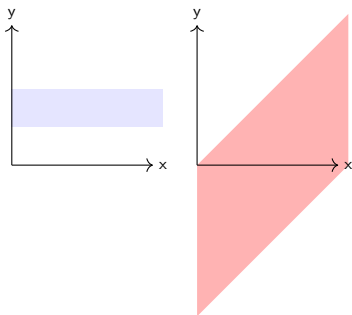
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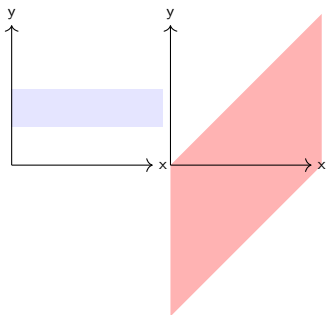
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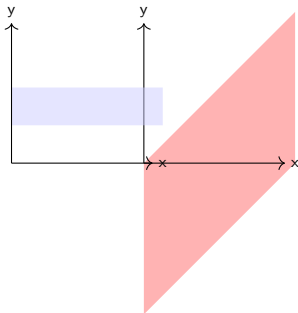
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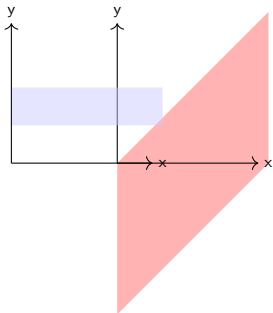
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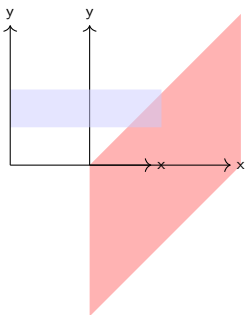
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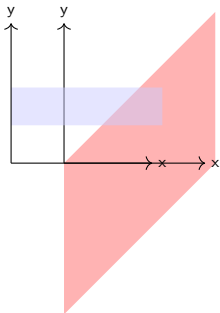
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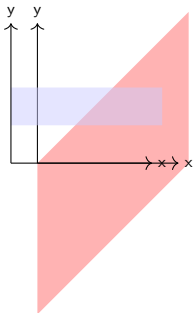
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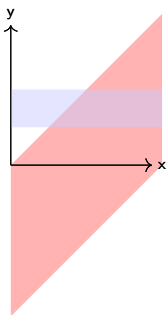
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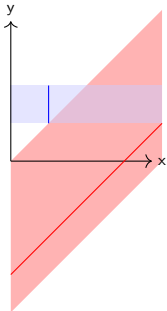
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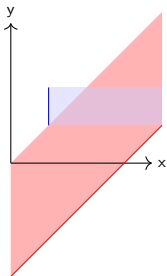
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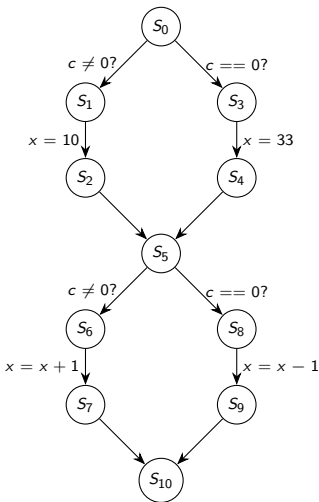
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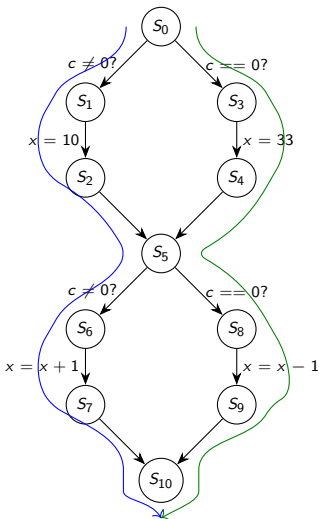


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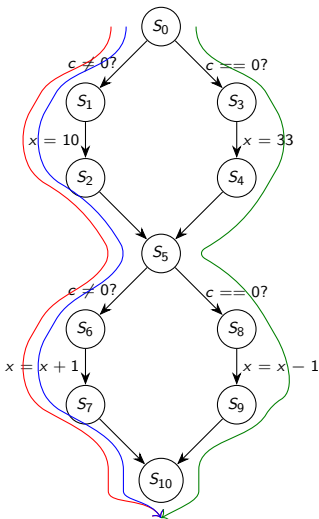
| | S_5 | S_6 | S_8 | S_{10} |
|-----|--------------|--------------|----------|--------------|
| c | \mathbb{Z} | \mathbb{Z} | 0 | \mathbb{Z} |
| x | [10; 33] | [10; 33] | [10; 33] | [9; 34] |

- ▶ Consider several abstract traces separately...
- ▶ ...At least for some time
- ✓ More precise than collecting semantics
- ✗ Finding appropriate partition is difficult



| | S_5 | S_6 | S_8 | S_{10} |
|-----|--------------|--------------|-------|--------------|
| c | 0 | \perp | 0 | 0 |
| x | 33 | \perp | 33 | 32 |
| c | \mathbb{Z} | \mathbb{Z} | 0 | \mathbb{Z} |
| x | 10 | 10 | 10 | [9; 11] |

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| | S_5 | S_6 | S_8 | S_{10} |
|-----|-----------------|-----------------|---------|-----------------|
| c | 0 | \perp | 0 | 0 |
| x | 33 | \perp | 33 | 32 |
| c | $[1; +\infty]$ | $[1; +\infty]$ | \perp | $[1; +\infty]$ |
| x | 10 | 10 | \perp | 11 |
| c | $[-\infty; -1]$ | $[-\infty; -1]$ | \perp | $[-\infty; -1]$ |
| x | 10 | 10 | \perp | 11 |

- ▶ Consider several abstract traces separately...
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Context

Overview of Static Analysis

Analyzing C code with Frama-C

- The Frama-C platform

- ACSL

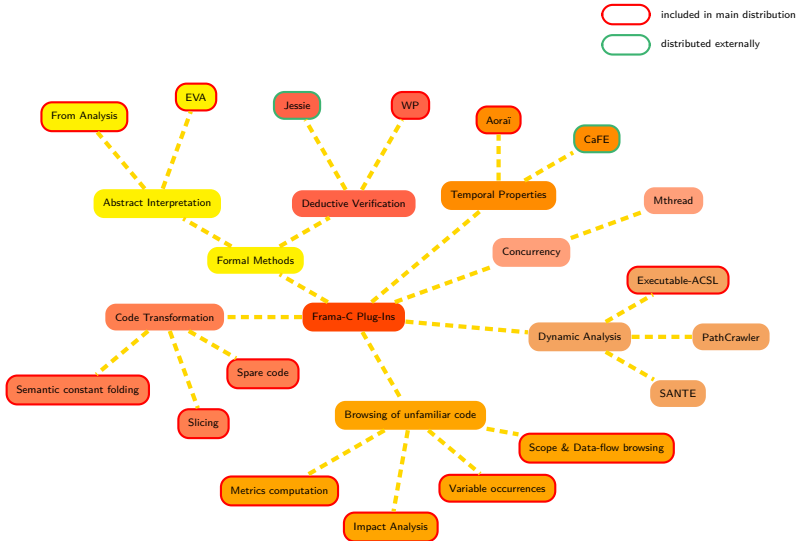
- Frama-C for Software Assessment

EVA Plugin

A few tools

- ▶ **Polyspace Verifier**: check absence of runtime errors (C/C++/Ada)
<https://fr.mathworks.com/products/polyspace.html>
- ▶ **ASTRÉE**: absence of runtime errors **without false alarm** in
SCADE-generated code <https://www.absint.com/astree/index.htm>
- ▶ **Verasco**: certified (in Coq) analyzer <http://compcert.inria.fr/verasco/>
- ▶ **aiT/StackAnalyzer**: WCET and stack size (assembly code)
<https://www.absint.com/ait/>
- ▶ **FLUCTUAT**: accuracy of floating-point computations and origin of
rounding errors <http://www.lix.polytechnique.fr/~putot/fluctuat.html>
- ▶ **Frama-C**: platform for analyzing C code, including through
abstract interpretation <https://frama-c.com>

- ▶ A Framework for modular analysis of C code.
- ▶ <http://frama-c.com/>
- ▶ Developed at CEA Tech List and Inria
- ▶ Released under LGPL license (v17.0 Chlorine in June 2018)
- ▶ Kernel based on CIL (Necula et al. – Berkeley).
- ▶ ACSL annotation language.
- ▶ Extensible platform
 - ▶ Collaboration of analyses over same code
 - ▶ Inter plug-in communication through ACSL formulas.
 - ▶ Adding specialized plug-in is easy



Main role

- ▶ Parsing and pretty-printing C code
- ▶ Manage internal state of plugins
- ▶ Manage properties status
- ▶ Orchestrate inter-plugins collaboration
- ▶ Save and load internal state

Example

```
frama-c examples/code.c \  
    -val -main f \  
    -then -wp \  
    -then -save code.sav  
frama-c-gui -load code.sav  
frama-c -load code.sav -report
```

Presentation

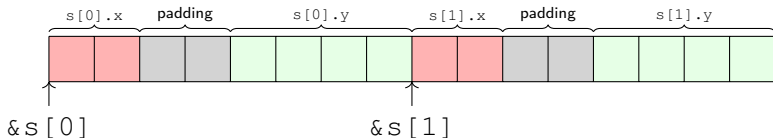
- ▶ Based on the notion of contract, like in Eiffel
- ▶ Allows users to specify functional properties of their code
- ▶ Allows communication between various plugins
- ▶ Independent from a particular analysis
- ▶ ACSL manual at
<https://github.com/acsl-language/acsl/releases>

Basic Components

- ▶ First-order logic
- ▶ Pure C expressions
- ▶ C types + \mathbb{Z} (integer) and \mathbb{R} (real)
- ▶ Built-ins predicates and logic functions, particularly over pointers.

- ▶ All operations are done over \mathbb{Z} : **no overflow**
- ▶ ACSL predicate $\text{INT_MIN} \leq x + y \leq \text{INT_MAX}$
 \Leftrightarrow
C operation $x+y$ does not overflow (undefined behavior)
- ▶ $(\text{int})z \equiv z \bmod 2^{8*\text{sizeof}(\text{int})}$
- ▶ and $\text{INT_MIN} \leq (\text{int})z \leq \text{INT_MAX}$

- ▶ Operations over \mathbb{R} : *infinite precision*
- ▶ `\round_double`(*r*, `\NearestEven`) to explicitly choose rounding mode
- ▶ predicates `\is_finite`(*d*), `\is_plus_infinity`(*d*), `\is_NaN`(*d*), ...
- ▶ function `\exact`(*x*): the value that C variable *x* would have if all computations had been done using \mathbb{R} . `\round_error` is the distance between *x* and `\exact`(*x*)
- ▶ typical specification:
`\round_error(\result) <= acceptable_limit`



```
struct S {  
  short x;  
  int y;  
} s[2];
```

```
\valid(&s[0]+(0 .. 1))  
\valid((char*)&s[0] + (0 .. 15))  
\!initialized(*( (char*)&s[0].x+2))  
\block_length(&s[0]) == 16  
\base_addr(&s[0].y) == s  
\offset(&s[1].y) == 12  
\separated(&s[0], &s[1])
```

Question

If we have `\valid(p+(0 .. 2))`, with `p` a pointer to `int`, and `sizeof(int)==4`, what can we say about `\block_length(p)`?

Answers

- a `\block_length(p) == 2`
- b `\block_length(p) == 3`
- c `\block_length(p) == 8`
- d `\block_length(p) == 12`
- e `\block_length(p) >= 12`

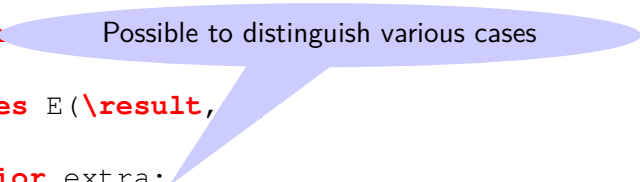
[◀ Back to presentation](#)[▶ See solution](#)[▶▶ Skip quiz](#)


```
/*@ requires R(x);  
  
    ensures E(\result, x);  
  
    behavior extra:  
        assumes A(x);  
        ensures more_result(\result, x);  
*/  
int f(int x);
```

What is required from caller

```
/*@ requires R(x);  
  
    ensures E(\result, x);  
  
    behavior extra:  
        assumes A(x);  
        ensures more_res;  
*/  
int f(int x);
```

What the function guarantees when returning successfully

```
/*@ require  Possible to distinguish various cases  
ensures E(\result,  
  
behavior extra:  
    assumes A(x);  
    ensures more_result(\result,x);  
*/  
int f(int x);
```

Question

Assuming an ACSL function `acsl_strlen` that returns the offset of the first `'\0'` char if it exists and `-1` otherwise, what would be an appropriate `requires` for the standard library function `size_t strlen(const char* s)`?

Answers

- a `acsl_strlen(s) >= 0`
- b `acsl_strlen(s) >= 0 && \valid(s+ (0 .. acsl_strlen(s)))`
- c `\valid(s + (0 .. acsl_strlen(s)))`
- d `acsl_strlen(s) >= 0 && \valid(s)`

```
/*@ assert p == NULL || \valid(p); */  
if (p) { *p = 42; }  
  
if (0) { /*@ assert \false; */ exit (1); }
```

Assess a property at given point

```
/*@ assert p == NULL || \valid(p); */  
if (p) { *p = 42; }
```

```
if (0) { /*@ assert \false; */ exit (1); }
```

Assess a property at given point

```
/*@ assert p == NULL || \valid(p); */  
if (p) { *p = 42; }  
  
if (0) { /*@ assert \false; */ exit (1); }
```

Indicates dead code

What is verified by Frama-C?

Code Properties

- ▶ Functional properties (contract)
- ▶ Absence of run-time error
- ▶ Dependencies
- ▶ Termination
- ▶ Non-interference
- ▶ Temporal properties

Perimeter of the verification

- ▶ Which part of the code is under analysis?
- ▶ Which initial context?

Trusted Code Base

- ▶ ACSL Axioms
- ▶ Hypotheses made by analyzers
- ▶ Stub Functions
- ▶ Frama-C itself

Context

Overview of Static Analysis

Analyzing C code with Frama-C

EVA Plugin

- Basics

- Refining Analysis

- Setting Analysis Context

Credits

- ▶ Pascal Cuoq
- ▶ Boris Yakobowski
- ▶ André Maroneze
- ▶ David Buhler
- ▶ Valentin Perrelle
- ▶ Matthieu Lemerre
- ▶ A few other developers...

More information

- ▶ <http://frama-c.com/download/frama-c-value-analysis.pdf>

Find the domains of the variables of a program

- ▶ based on **abstract interpretation**
- ▶ **alarms** on operations that **may** be invalid
- ▶ alarms on the specifications that may be invalid
- ▶ **Correct**: if no alarm is raised, no runtime error can occur

- ▶ Precise handling of **pointers**
- ▶ Several representation for dynamic allocation (precision vs. time)
- ▶ time and memory efficient (as much as achievable)
- ▶ Precise enough
 - ▶ for proving absence of runtime errors on some critical code
 - ▶ to serve as a back-end for other semantical analyzes through its API

Corresponding Abstract Domain

- small set of integers (by default, cardinal ≤ 8)
- \oplus integer interval \times modulo information
- \oplus finite floating-point interval

Examples

- ▶ $\{0; 40; \}$ = 0 or 40
- ▶ $[0..40]$ = an integer between 0 and 40 (inclusive)
- ▶ $[-..-]$ = any integer (within the bound of the corresponding integral type)
- ▶ $[3..39], 3\%4$ = 3, 7, 11, 15, 19, 23, 27, 31, 35 or 39
- ▶ $[0.25..3.125]$ = floating-point between 0.25 and 3.125 (inclusive)

```
int x, y, t, m; double d;
extern char z; char z1;

void f(int c) {
    if (c) x = 40;
    for (int i = 0; i<=40; i++) {
        Frama_C_show_each_loop_1(i);
        if (c == i) y = i; }
    z1 = z;
    t = z;
    m=3;
    for (int i = 3; i<=40; i+=4) {
        if (c == i) m = i; }
    if (c) { d = 0.25; } else { d = 3.125; }
}
```

```
frama-c -val -main f integer.c
```

```
[value] Called Frama_C_show_each_loop_1({0; 1})
[value] Called Frama_C_show_each_loop_1({0; 1; 2})
[value] Called Frama_C_show_each_loop_1([0..16])
[value] Called Frama_C_show_each_loop_1([0..40])
[value] ===== VALUES COMPUTED =====
  x IN {0; 40}
  y IN [0..40]
  z1 IN [--..--]
  t IN [-128..127]
  m IN [3..39], 3%4
  d IN [0.25 .. 3.125]
```

Question

if x is in the interval $[-10 \dots 10]$ before the execution of statement

```
if (x==0) { y = 14; }
else { y = x<0 ? 13 : x + 2; }
```

What is the value associated to y after the statement?

Answers

- a $[-8 \dots 14]$
- b $[2 \dots 13]$
- c $[2 \dots 14]$
- d $[3 \dots 14]$

Base Address

Global variable

- ⊕ Formal parameter of main function
- ⊕ literal string constant
- ⊕ NULL
- ⊕ ...

Addresses

- ▶ Base address + Offset (integer)
- ▶ Each base has a maximal valid offset
- ▶ Abstract Values are sets of addresses

Precise Base

- ▶ $\{\{\&p + \{4; 8\}\}\}$ = address of p shifted from 4 or 8 octets
- ▶ $\{\{\&"foobar"; \}\}$ = Address of literal string "foobar" (shifted from 0)
- ▶ $\{\{\&NULL + \{1024; \}\}\}$ = Absolute location 1024

Imprecision

- ▶ garbled mix of $\&\{x_1; \dots; x_n\}$ = unknown address built upon arithmetic operations over integers and addresses $x_1; \dots; x_n$.
- ▶ ANYTHING = top of the lattice. Should not occur in practice

```
int* x,*z, *t; const char* y; int p[3];
const char* string = "foobar";
```

```
void f(int c) {
    if (c) { x = &p[1]; }
    else { x = &p[2]; }
    y = string;
    z = (int*)1024;
    t = (int*) ((int)x | 4096);
}
```

```
[value] ===== VALUES COMPUTED =====  
[value] Values at end of function f:  
  x IN {{ &p{[1], [2]} }}  
  y IN {{ "foobar" }}  
  z IN {1024}  
  t IN  
    {{ garbled mix of &{p}  
      (origin: Arithmetic  
        {examples/value/address.c:16}) }}
```

Abstract Domain

written address = valid left value

- address
- × initialized?
- × *not dangling pointer?*

Example

```

int x, y;
if (e) x = 2;
L: if (e) y = x + 1;
  
```

- ▶ At L , we know that x equals 2 iff it has been initialized
- ▶ Depending on the complexity of e , we know that y equals 3 if x equals 2

```

int X,Y, *p;
void f(int c) {
    int x,y;
    if (c<=0) x = 2;
L:  if (c<=0) y = x + 1; else y = 4;
    X = x;
    Y = y;
    p = c ? &X : &x;
}

int main(int c) {
    f(c);
    if (Y==4) *p = 3;
    return 0;
}
  
```

```
examples/value/address_written.c:8:  
[kernel] warning:  
    accessing uninitialized left-value:  
    assert \initialized(&x);  
examples/value/address_written.c:16:  
[kernel] warning:  
    accessing left-value that  
    contains escaping addresses:  
    assert !\dangling(&p);  
[value] Values at end of function main:  
X IN {2; 3} or UNINITIALIZED  
Y IN {3; 4}  
p IN {{ &X }} or ESCAPINGADDR  
__retres IN {0}
```

Question

if a is an array of size 3, initialized to 0, and c in $[0 \dots 2]$ what would be the content of a after executing the following statement:

```
if (c) { a[c] = c; } else a[1] =3;
```

Answers

a $a[0] \text{ IN } \{0\}, a[1] \text{ IN } \{0,1,3\}, a[2] \text{ IN } \{0,2\}$

b $a[i] \text{ IN } \{0,1,2,3\}$ for all indices

c

$a[0] \text{ IN } \{0\}, a[1] \text{ IN } \{0,1,2,3\} a[2] \text{ IN } \{0,1,2\}$

d $a[0] \text{ IN } \{0\}, a[1] \text{ IN } \{1,3\}, a[2] \text{ IN } \{2\}$

- ▶ New domains can provide additional information:
 - ▶ equalities between values
 - ▶ values of symbolic locations
 - ▶ gauges, affine relation wrt number of loop steps
- ▶ Possible to add new domains
- ▶ Inter-domain communication done through **queries**:

```

val extract_expr :
  (exp -> value evaluated) ->
  state -> exp -> (value * origin) evaluated
  
```

```

val extract_lval :
  (exp -> value evaluated) ->
  state -> lval -> typ -> location -> (value * o
  
```

```
#include "___fc_builtin.h"

int main () {
    int x = Frama_C_interval(0,10);
    int y = x;
    if ( y <= 5) {
        return x;
    } else {
        return 10 - x;
    }
}
```

Main options

- ▶ option `-slevel`: allows EVA to explore n separated paths before joining them
- ▶ option `-slevel-function`: same as previous, but for a particular function
- ▶ annotation `loop pragma UNROLL`: syntactic loop unrolling
- ▶ annotation `loop pragma WIDEN HINTS`: give bounds for widening

For specialists only

- ▶ option `-ilevel`: maximum number of elements in the set before conversion into intervals
- ▶ option `-plevel`: maximum number of distinct array cells

Driving Value through Annotations

▶ **ACSL assertions** can be used to restrict propagated domains

▶ but only if Value can interpret it

```
/*@ assert x % 2 == 0; */
```

```
// potentially useful
```

```
/*@ assert \exists integer y; x == 2 * y; */
```

```
// useless
```

▶ Case analysis using **disjunctions**

```
int S=0;

int T[5];

int main(void) {
    int i;
    int *p = &T[0] ;
    for (i = 0; i < 5; i++) {
        S = S + i; *p++ = S;
    }
    return S;
}
```

```
int x,y;

void main (int c) {
    if (c) { x = 10; } else { x = 33; }
    if (!c) { x++; } else { x--; }

    if (c<=0) { y = 42; } else { y = 36; }
    if (c>0) { y++; } else { y--; }
}
```

without level

```
x IN {9; 11; 32; 34}
y IN {35; 37; 41; 43}
```

with level, no assertion

```
x IN {9; 11; 34}
y IN {37; 41}
```

with level and assertion

```
/*@ assert c<=0 || c > 0; */
```

```
[value] Assertion got status valid.
```

```
x IN {9; 34}
y IN {37; 41}
```

- ▶ Which part of the code should be analyzed?
- ▶ `-main f` starts the analysis at function `f`
- ▶ `-lib-entry` indicates that the the initial global context is **not** 0-initialized
- ▶ `-context-width`, `-context-depth`
- ▶ Use of a driver function with some builtins to provide non-determinism:

```
void f_wrapper() {  
    setup_analysis_context();  
    f(arg_1, arg_2);  
}
```



```
int search(char* a, char key) {  
    char* orig = a;  
    while (*a) {  
        if (*a == key) return a - orig;  
        a++;  
    }  
    return -1;  
}
```

```
frama-c -val -context-width 3 -main search context.c
```

```
[...]
```

```
context.c:3:[kernel] warning: out of bounds read. ass
```

```
context.c:4:[kernel] warning: out of bounds read. ass
```

```
context.c:4:[kernel] warning: pointer subtraction:
```

```
    assert \base_addr(a) == \base_addr(orig);
```

```
[value] Recording results for search
```

```
[value] done for function search
```

```
[value] ===== VALUES COMPUTED =====
```

```
[value] Values at end of function search:
```

```
  a IN {{ &S_a{[0], [1], [2]} }}
```

```
  orig IN {{ NULL ; &S_a[0] }}
```

```
  __retres IN {-1; 0; 1; 2}
```

```
#include "__fc_builtin.h"
#include "limits.h"

int search(char* a, char key);

char buffer[1024];

int driver() {
    buffer[1023] = 0;
    char key = Frama_C_interval(CHAR_MIN, CHAR_MAX);
    return search(buffer, key);
}
```

```
frama-c -val -context-width 3 -main driver \  
        context.c context_driver.c -lib-entry \  
        -slevel 1024
```

```
[ ... No alarm ... ]
```

```
[value] Values at end of function search:
```

```
  a IN {{ &buffer + [0..1023] }}  
  orig IN {{ &buffer[0] }}  
  __retres IN [-1..1022]
```

```
[value] Values at end of function driver:
```

```
  Frama_C_entropy_source IN [--..--]  
  buffer[0..1022] IN [--..--]  
    [1023] IN {0}  
  key IN [--..--]
```

Provide an “implementation” for EVA

- ▶ Assumed to match the real implementation
- ▶ Write stub directly in C (aimed at ease of analysis, not performance)
- ▶ Provide an ACSL specification
- ▶ `-val-use-spec f`
- ▶ Use an EVA built-in (`-val-builtin`)
- ▶ `-val-builtins-list`

Command-line Options

- ▶ `-val-ignore-recursive-calls` assumes recursive calls have no effect
- ▶ `-all-rounding-modes` do not assume floating-point computations use same rounding as host machine

ACSL Properties

- ▶ Alarms emitted by Value
- ▶ Annotations with `Unknown` status

CERT ARR30-C bad code sample

```
static int *table = NULL;
static size_t size = 0;

int insert_in_table(size_t pos, int value) {
    if (size < pos) {
        int *tmp;
        size = pos + 1;
        tmp = (int *)realloc(table, sizeof(*table) * size);
        if (tmp == NULL) {
            return -1;    /* Failure */
        }
        table = tmp;
    }
    table[pos] = value;
    return 0;
}
```

- ▶ D. Delmas and J. Souyris: ASTRÉE: from Research to Industry, SAS 2007
- ▶ TrustInSoft startup (created 2013): <https://trust-in-soft.com/>
- ▶ A. Ourghanlian: Evaluation of static analysis tools used to assess software important to nuclear power plant safety. In Nuclear Engineering and Technology, vol 47 issue 2, 2015.
- ▶ INGOPCS project: <https://www.ingopcs.net>
- ▶ Open-Source Case Studies:
<https://github.com/Frama-C/open-source-case-studies>
- ▶ A. Maroneze: Analysis of the Chrony NTP server.
<http://blog.frama-c.com/index.php?post/2018/06/19/Analyzing-Chrony-with-Frama-C/Eva>

Context

Overview of Static Analysis

Analyzing C code with Frama-C

EVA Plugin

General

- ▶ Correnson &al. Frama-C User Manual (v17 - Chlorine). May 2018
- ▶ Kirchner &al. Frama-C, a Software Analysis Perspective, vol 37 of Formal Aspects of Computing, March 2015.

ACSL

- ▶ Baudin &al. ACSL: ANSI/ISO C Specification Language. Preliminary Design (v 1.13). May 2018
- ▶ Burghardt &al. ACSL by Example (v16.1). December 2017.

<https://github.com/fraunhoferfokus/acsl-by-example>

EVA

- ▶ Cuoq &al. Frama-C's value analysis plug-in. May 2018
- ▶ Blazy &al. Structuring Abstract Interpreters through State and

Course

- ▶ Patrick Cousot, MIT 2005

<http://web.mit.edu/afs/athena.mit.edu/course/16/16.399/www/>

Books

- ▶ Hanne Nielson, Flemming Nielson, and Chris Hankin. *Principles of Program Analysis*. Springer 1999
- ▶ Neil Jones and Flemming Nielson, *Abstract Interpretation: a Semantics-Based Tool for Program Analysis*. In *Handbook of Logic in Computer Science, vol. 4*, Oxford University Press 1994

Founding Articles

- ▶ Patrick and Radhia Cousot, *Abstract Interpretation: a Unified Lattice Model for Static Analysis of Programs by Construction or Approximation of Fixpoints*. PoPL'77
- ▶ Patrick Cousot and Nicolas Halbwachs, *Automatic Discovery of Linear Restraints Among Variables of a Program*. PoPL'78
- ▶ Patrick and Radhia Cousot, *Systematic Design of Program Analysis Frameworks*. PoPL'79
- ▶ <http://www.di.ens.fr/~cousot/COUSOTpapers.shtml>

Solutions to Quizzes

Question

We have information from two domains:

Intervals:

▶ $x \in [0; 20]$

▶ $y \in [5; 10]$

Octagons:

$$0 \leq x - y \leq 20$$

What can be said about x and y ?

Answers

▶ a $x \in [0; 20], y \in [5; 10]; 0 \leq x - y \leq 20$ ✗

▶ b $x \in [5; 20], y \in [5; 10], 0 \leq x - y \leq 15$

▶ c $x \in [5; 20], y \in [5; 10], 0 \leq x - y \leq 10$

▶ d $x \in [5; 20], y \in [0; 20], 0 \leq x - y \leq 20$

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▶ d $x \in [5; 20], y \in [0; 20], 0 \leq x - y \leq 20$ ✗

Question

If we have `\valid(p+(0 .. 2))`, with `p` a pointer to `int`, and `sizeof(int)==4`, what can we say about `\block_length(p)`?

Answers

- a `\block_length(p) == 2` ❌
- b `\block_length(p) == 3`
- c `\block_length(p) == 8`
- d `\block_length(p) == 12`
- e `\block_length(p) >= 12`

◀ Back to presentation

▶ See solution

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[◀ Back to presentation](#)
[▶ See solution](#)

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- d `\block_length(p) == 12` **X**
- e `\block_length(p) >= 12`

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◀ Back to presentation

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Question

Assuming an ACSL function `acsl_strlen` that returns the offset of the first `'\0'` char if it exists and `-1` otherwise, what would be an appropriate `requires` for the standard library function `size_t strlen(const char* s)`?

Answers

- ▶ a `acsl_strlen(s) >= 0` ❌
- ▶ b `acsl_strlen(s) >= 0 && \valid(s+ (0 .. acsl_strlen(s)))`
- ▶ c `\valid(s + (0 .. acsl_strlen(s)))`
- ▶ d `acsl_strlen(s) >= 0 && \valid(s)`

Question

Assuming an ACSL function `acsl_strlen` that returns the offset of the first `'\0'` char if it exists and `-1` otherwise, what would be an appropriate `requires` for the standard library function `size_t strlen(const char* s)`?

Answers

- a `acsl_strlen(s) >= 0`
- b `acsl_strlen(s) >=0 &&`
- c `\valid(s+ (0 .. acsl_strlen(s)))`
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Question

Assuming an ACSL function `acsl_strlen` that returns the offset of the first `'\0'` char if it exists and `-1` otherwise, what would be an appropriate `requires` for the standard library function `size_t strlen(const char* s)`?

Answers

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Question

if x is in the interval $[-10 \dots 10]$ before the execution of statement

```

if (x==0) { y = 14; }
else { y = x<0 ? 13 : x + 2; }
  
```

What is the value associated to y after the statement?

Answers

- a $[-8 \dots 14]$ **X**
- b $[2 \dots 13]$
- c $[2 \dots 14]$
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if a is an array of size 3, initialized to 0, and c in $[0 \dots 2]$ what would be the content of a after executing the following statement:

```
if (c) { a[c] = c; } else a[1] =3;
```

Answers

a $a[0] \in \{0\}$, $a[1] \in \{0,1,3\}$, $a[2] \in \{0,2\}$

X

b $a[i] \in \{0,1,2,3\}$ for all indices

c

$a[0] \in \{0\}$, $a[1] \in \{0,1,2,3\}$ $a[2] \in \{0,1,2\}$

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b `a[i] IN {0,1,2,3} for all indices` ✗

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`a[0] IN {0}, a[1] IN {0,1,2,3} a[2] IN {0,1,2}`

d `a[0] IN {0}, a[1] IN {1,3}, a[2] IN {2}`

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